

CEMMAC

Centro Multidisciplinario de Modelación Matemática
y Computacional

3er
WORKSHOP
CEMMAC 2018

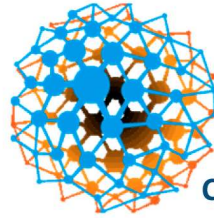
Modelación Matemática y sus
Aplicaciones a la Medicina y Biología

27 y 28 de Septiembre Auditorio "Joaquín Ancona", FCFM-BUAP Puebla, México



BUAP

Facultad de Ciencias Físico Matemáticas



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y Computacional



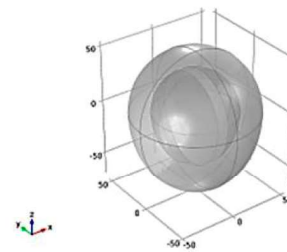
INVITA AL

Taller 2:

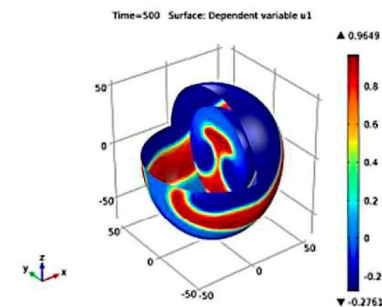
Introducción a la Simulación usando COMSOL Multiphysics 3^{er} WORKSHOP CEMMAC 2018

El objetivo de este taller es programar en COMSOL Multiphysics la ecuación de Poisson, la ecuación de calor y la ecuación de onda, las cuales son, en muchos casos, las bases de simulaciones de fenómenos físicos más complejos.

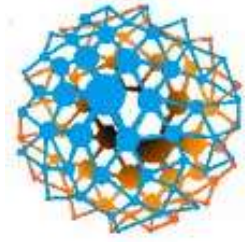
En este taller aprenderás las herramientas básicas para poder generar un dominio y su mallado; así como a programar las condiciones de frontera y condiciones iniciales que se requieran. Además, conocerás las diferentes opciones que COMSOL Multiphysics tiene para visualizar los resultados y podrás guardar las imágenes y videos de las simulaciones.



Model Geometry: A heart is represented by two semispherical cavities.



Solution of the FitzHugh-Nagumo equations for the activation potential at time $t = 500$ seconds.



CEMAC

Introducción a la simulación usando COMSOL Multiphysics.

Dra. Beatriz Bonilla Capilla

Catedrática de CONACYT

Centro Multidisciplinario de Modelación Matemática y Computacional

Facultad de Ciencias Físico Matemáticas

Benemérita Universidad Autónoma de Puebla



Second order PDEs

$$a \frac{\partial^2 u}{\partial x^2} + 2b \frac{\partial^2 u}{\partial x \partial y} + c \frac{\partial^2 u}{\partial y^2} + d \frac{\partial u}{\partial x} + e \frac{\partial u}{\partial y} + f u = g.$$

$$a u_{xx} + b u_{xy} + c u_{yy} + d u_x + e u_y + f u = g(x,y).$$

For the equation to be of second order, a , b , and c cannot all be zero. Define its *discriminant* to be $b^2 - 4ac$. The properties and behavior of its solution are largely dependent of its *type*, as classified below.

If $b^2 - 4ac > 0$, then the equation is called *hyperbolic*. The wave equation is one such example.

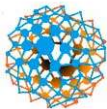
If $b^2 - 4ac = 0$, then the equation is called *parabolic*. The heat conduction equation is one such example.

If $b^2 - 4ac < 0$, then the equation is called *elliptic*. The Laplace equation is one such example.

$$\alpha^2 u_{xx} = u_t \quad (\text{one-dimensional heat conduction equation})$$

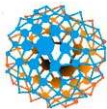
$$a^2 u_{xx} = u_{tt} \quad (\text{one-dimensional wave equation})$$

$$u_{xx} + u_{yy} = 0 \quad (\text{two-dimensional Laplace/potential equation})$$

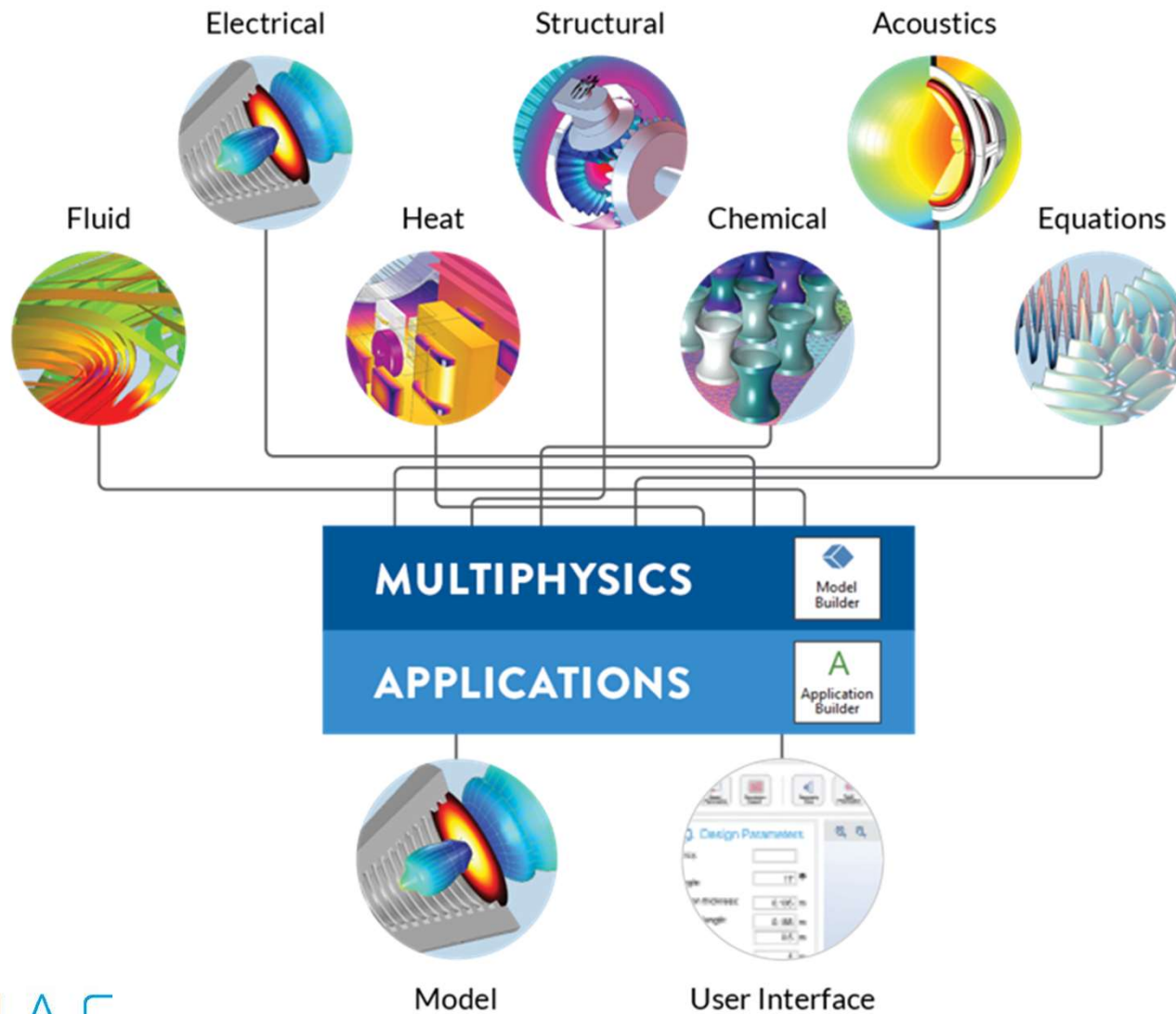


Ecuación Diferencial Parcial de segundo orden.

- Dominio
- Condiciones de Frontera:
 - Dirichlet
 - Newman
- Condiciones Iniciales



COMSOL Multiphysics

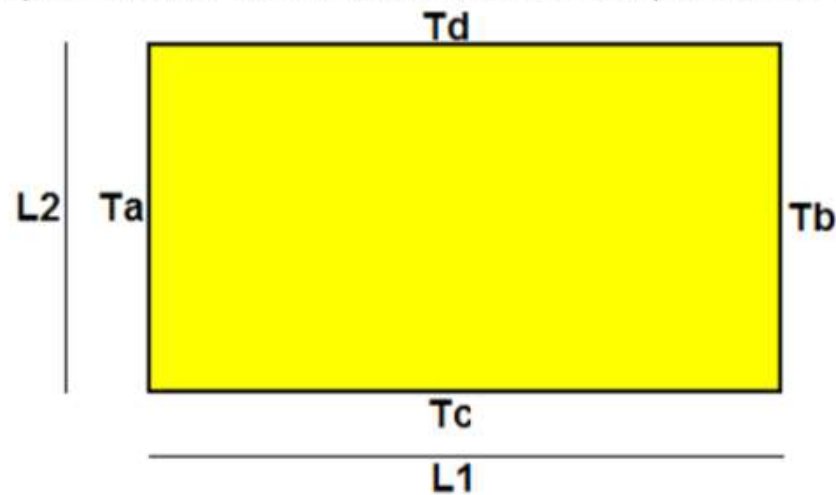


Ejemplo. Resolver la ecuación de difusión en dos dimensiones:

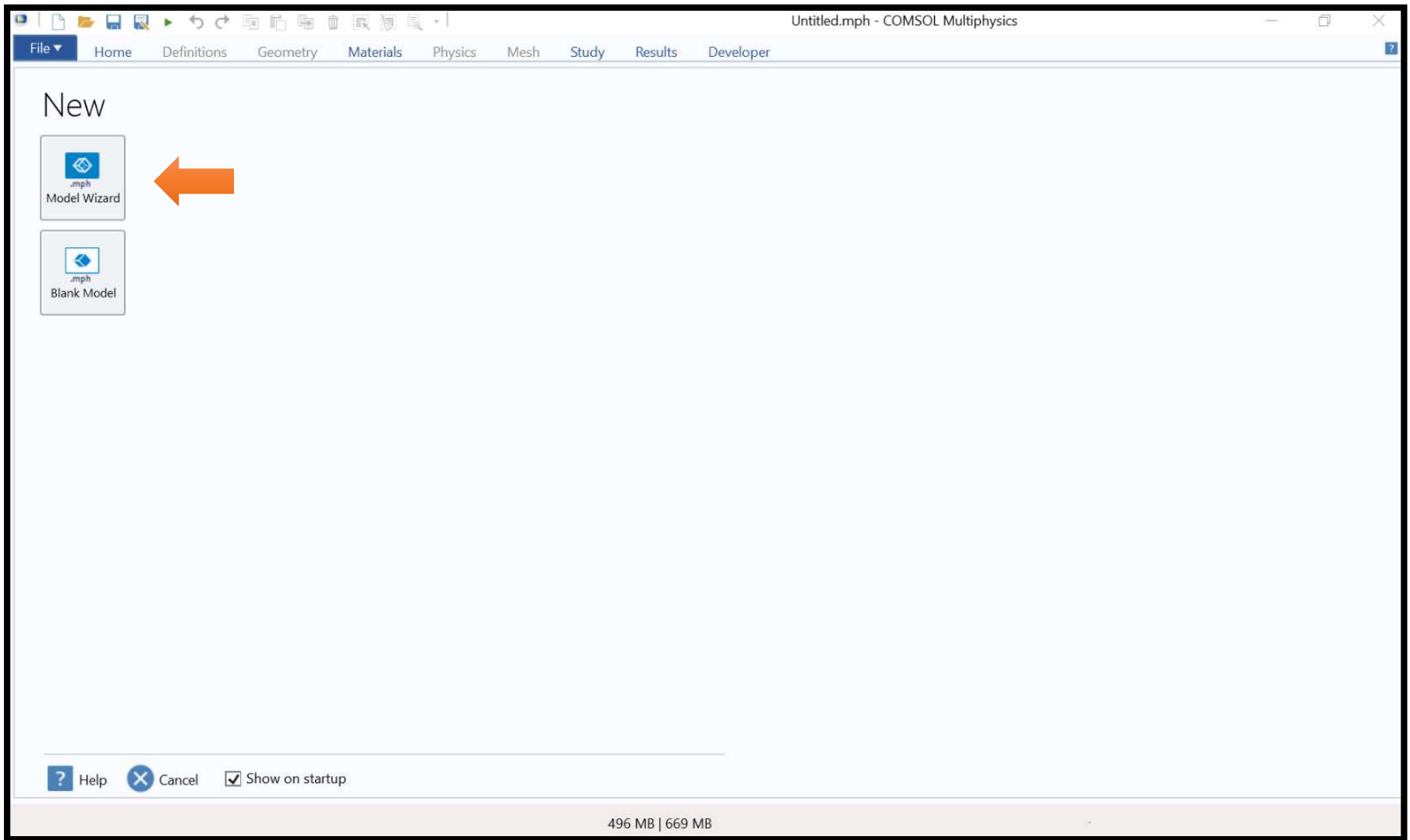
$$u(x,y): \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$$

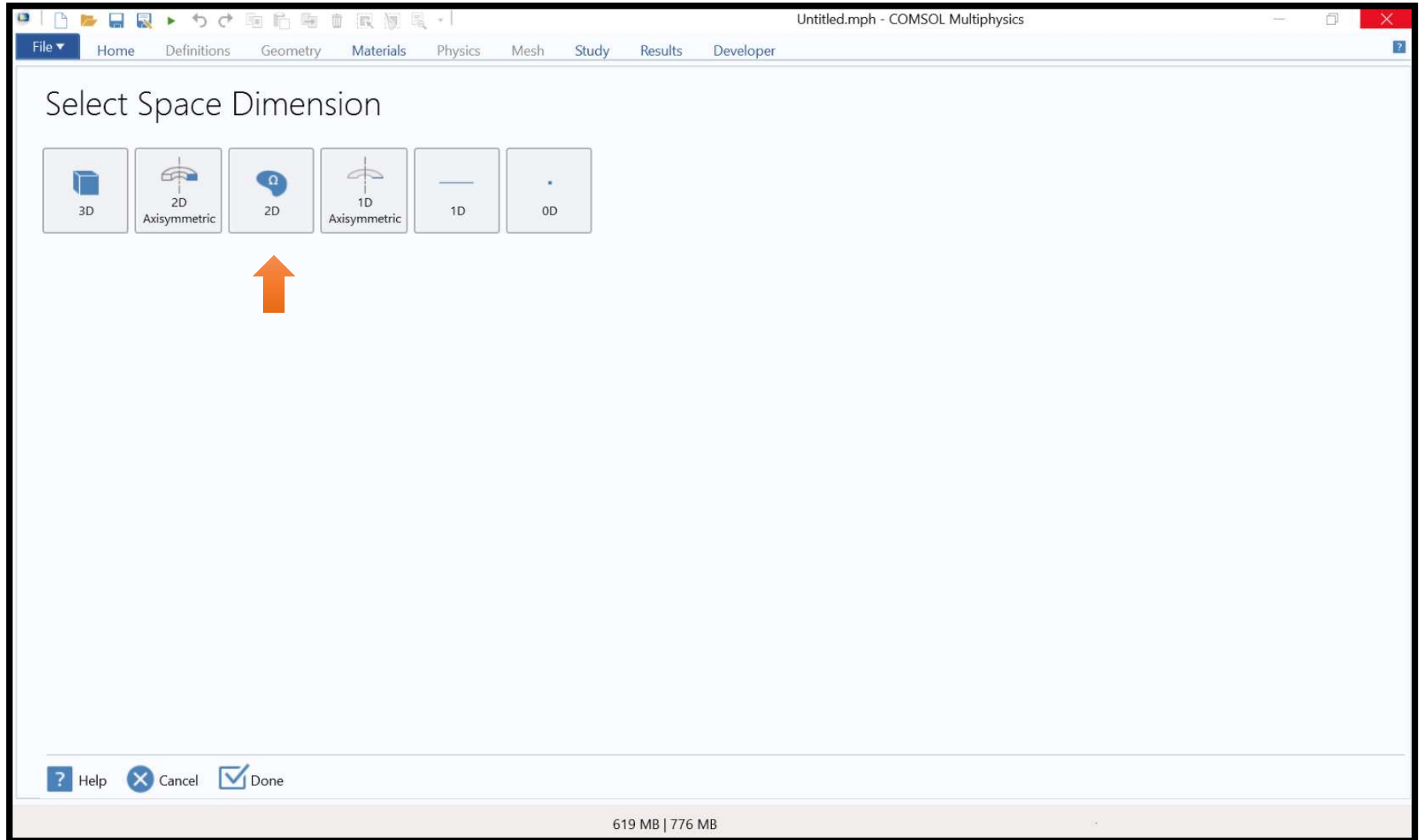
Suponer que u es una función que depende de x, y , en donde u representa valores de temperatura, x, y representan posición.

Esta ecuación se puede asociar al flujo de calor en una placa muy delgada aislada térmicamente en sus caras superior e inferior y sometida en los bordes a alguna condición. La solución representa la distribución final de temperaturas en la placa en cada punto (x, y)



T_a, T_b, T_c, T_d son valores de temperatura, suponer constantes, de alguna fuente de calor aplicada en cada borde de la placa. $L1, L2$ son las dimensiones de la placa.





calor2D.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Select Physics

Search

- Plasma
- Radio Frequency
- Semiconductor
- Structural Mechanics
- Mathematics**
 - PDE Interfaces
 - Coefficient Form PDE (c)
 - General Form PDE (g)
 - Wave Form PDE (wahw)
 - Weak Form PDE (w)
 - PDE, Boundary Elements (pdebe)
 - Lower Dimensions
 - ODE and DAE Interfaces
 - Optimization and Sensitivity

Add

Added physics interfaces:

Remove

← Space Dimension → Study

Help Cancel Done

Mathematics

The Mathematics branch contains interfaces for solving PDEs and ODEs, performing sensitivity analysis, modeling moving meshes and deformed geometries, and more.

972 MB | 1193 MB

calor2D.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Select Physics

Search

- Plasma
- Radio Frequency
- Semiconductor
- Structural Mechanics
- Mathematics
 - PDE Interfaces
 - Coefficient Form PDE (c)
 - General Form PDE (g)
 - Wave Form PDE (wahw)
 - Weak Form PDE (w)
 - PDE, Boundary Elements (pdebe)
 - Lower Dimensions
 - ODE and DAE Interfaces
 - Optimization and Sensitivity

Add

Added physics interfaces:

- General Form PDE (g)

Remove

Review Physics Interface

General Form PDE (g)

Dependent Variables

Field name:

Number of dependent variables:

Dependent variables:

Units

Dependent variable quantity:

Source term quantity:

Unit:

← Space Dimension → Study

Help Cancel Done

941 MB | 1194 MB

calor2D.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Select Study

- Presets Studies
 - Eigenvalue
 - Stationary** ←
 - Time Dependent
- Custom Studies
 - Empty Study

Added study:

Stationary

Added physics interfaces:

General Form PDE (g)

Physics

Help Cancel Done ←

Stationary

The Stationary study is used when field variables do not change over time.

Examples: In electromagnetics, it is used to compute static electric or magnetic fields, as well as direct currents. In heat transfer, it is used to compute the temperature field at thermal equilibrium. In solid mechanics, it is used to compute deformations, stresses, and strains at static equilibrium. In fluid flow it is used to compute the steady flow and pressure fields. In chemical species transport, it is used to compute steady-state chemical composition in steady flows. In chemical reactions, it is used to compute the chemical composition at equilibrium of a reacting system.

It is also possible to compute several solutions, such as a number of load cases, or to track the nonlinear response to a slowly varying load.

948 MB | 1202 MB

Untitled.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Application Builder Component Parameters Functions Variables Geometry Materials

Build Mesh Mesh 1 Compute Add Study Study 1 Select Plot Group Add Plot Group Windows Reset Desktop

Model Builder Settings Graphics

Geometry Build All

Label: Geometry 1

Units

Scale values when changing units

Length unit: m

Angular unit: Degrees

Advanced

Default repair tolerance: Automatic

Automatic rebuild

Messages Progress Log

Finalized geometry is empty.
Saved file: C:\Users\Betty\Desktop\calor2D.mph
Finalized geometry has 1 domain, 4 boundaries, and 4 vertices.
Complete mesh consists of 310 domain elements and 46 boundary elements.
Complete mesh consists of 948 domain elements and 82 boundary elements.
Number of degrees of freedom solved for: 1979 (plus 168 internal DOFs).
Solution time (Study 1): 12 s.

955 MB | 1226 MB

Untitled.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder

- Untitled.mph (root)
 - Global Definitions
 - Materials
 - Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Mesh 1
 - Study 1
 - Step 1: Stationary
 - Results

Settings

Rectangle

Build Selected Build All Objects

Label: Rectangle 1

Object Type

Type: Solid

Size and Shape

Width: 2 m

Height: 1 m

Position

Base: Corner

x: 0 m

y: 0 m

Rotation Angle

Rotation: 0 deg

Layers

Selections of Resulting Entities

Contribute to: None New

Graphics

Messages Progress Log

Finalized geometry is empty.
 Saved file: C:\Users\Betty\Desktop\calor2D.mph
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 Complete mesh consists of 310 domain elements and 46 boundary elements.
 Complete mesh consists of 948 domain elements and 82 boundary elements.
 Number of degrees of freedom solved for: 1979 (plus 168 internal DOFs).
 Solution time (Study 1): 12 s.

960 MB | 1215 MB

Model Builder

Settings

General Form PDE

Override and Contribution

Equation

Show equation assuming:

Study 1, Stationary

$$e_a \frac{\partial^2 u}{\partial t^2} + d_a \frac{\partial u}{\partial t} + \nabla \cdot \Gamma = f$$

$$\nabla = \left[\frac{\partial}{\partial x}, \frac{\partial}{\partial y} \right]$$

Conservative Flux

Γ	-ux	x	1/m
	-uy	y	

Source Term

f 1 1/m²

Damping or Mass Coefficient

da 1 s/m²

Mass Coefficient

ea 0 s²/m²

Ejemplo. Resolver la ecuación de difusión en dos dimensiones:

$$u(x,y): \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$$

Suponer que u es una función que depende de x, y , en donde u representa valores de temperatura, x, y representan posición.

Untitled.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder

Settings

Dirichlet Boundary Condition

Label: Dirichlet Boundary Condition 1

Boundary Selection

Selection: Manual

Active

1

Override and Contribution

Equation

Dirichlet Boundary Condition

Prescribed value of u

r 320

Graphics

Messages Progress Log

Complete mesh consists of 948 domain elements and 82 boundary elements.
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 Complete mesh consists of 948 domain elements and 82 boundary elements.

922 MB | 1233 MB

Untitled.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings

Line Rectangle Circle Primitives

Booleans and Partitions Transforms Conversions

Chamfer Fillet Tangent

Virtual Operations

Parts Programming Other

Draw Operations Other

Model Builder

Settings

Mesh

Build All

Label: Mesh 1

Mesh Settings

Sequence type: Physics-controlled mesh

Element size: Finer

Graphics

Messages Progress Log

Complete mesh consists of 948 domain elements and 82 boundary elements.
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 Finalized geometry has 1 domain, 4 boundaries, and 4 vertices.
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922 MB | 1234 MB

Untitled.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Tangent Fillet Virtual Operations Parts Programming Other

Model Builder

- Untitled.mph (root)
 - Global Definitions
 - Materials
 - Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Dirichlet Boundary Condition 1
 - Dirichlet Boundary Condition 2
 - Dirichlet Boundary Condition 3
 - Dirichlet Boundary Condition 4
 - Mesh 1
 - Study 1
 - Step 1: Stationary
 - Results

Settings

Stationary

Compute ←

Label: Stationary

Study Settings

Results While Solving

Physics and Variables Selection

Modify physics tree and variables for study step

Physics interface	Solve for	Discretiz
General Form PDE (g)	<input checked="" type="checkbox"/>	Physic

Values of Dependent Variables

Mesh Selection

Adaptation and Error Estimates

Study Extensions

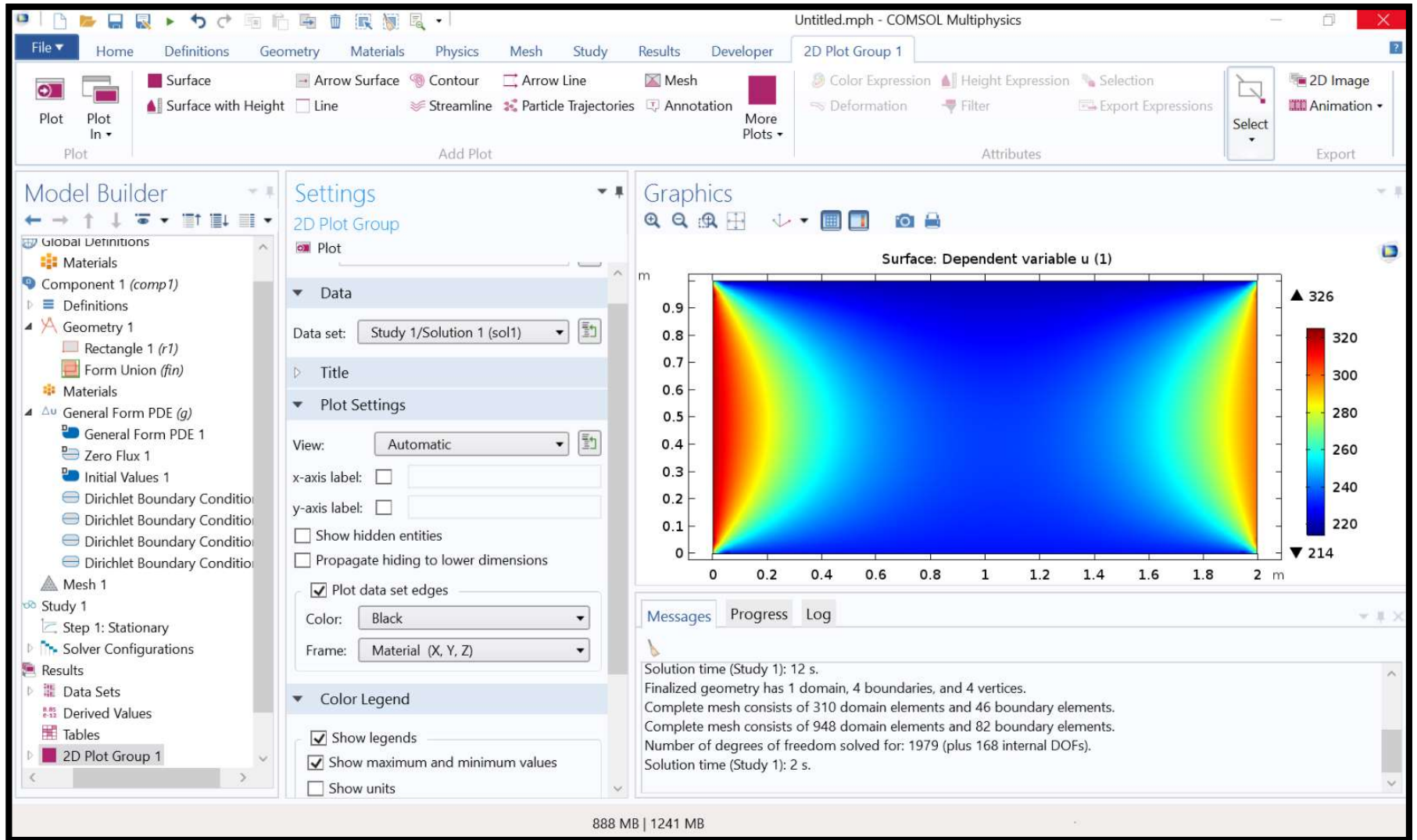
Graphics

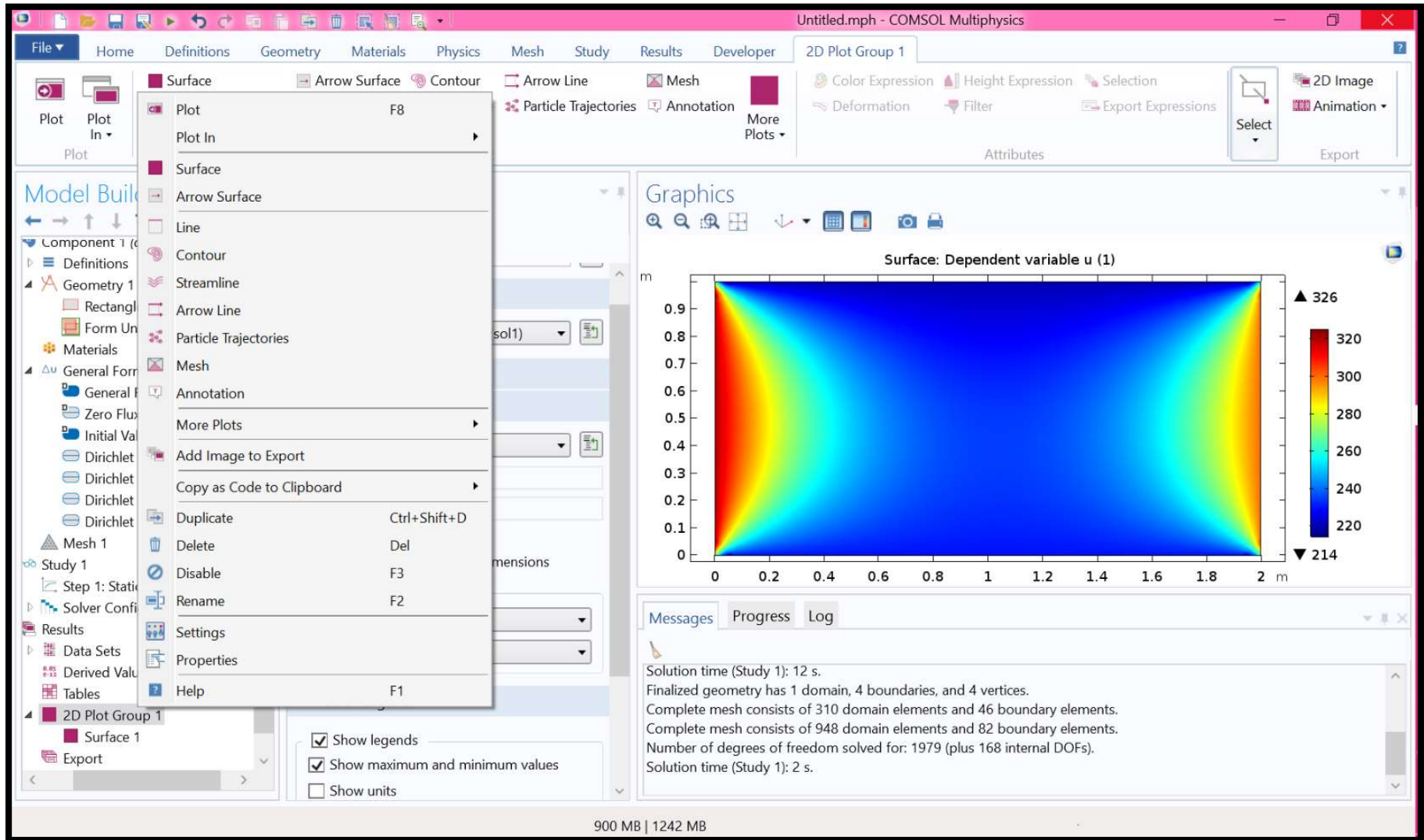
Messages Progress Log

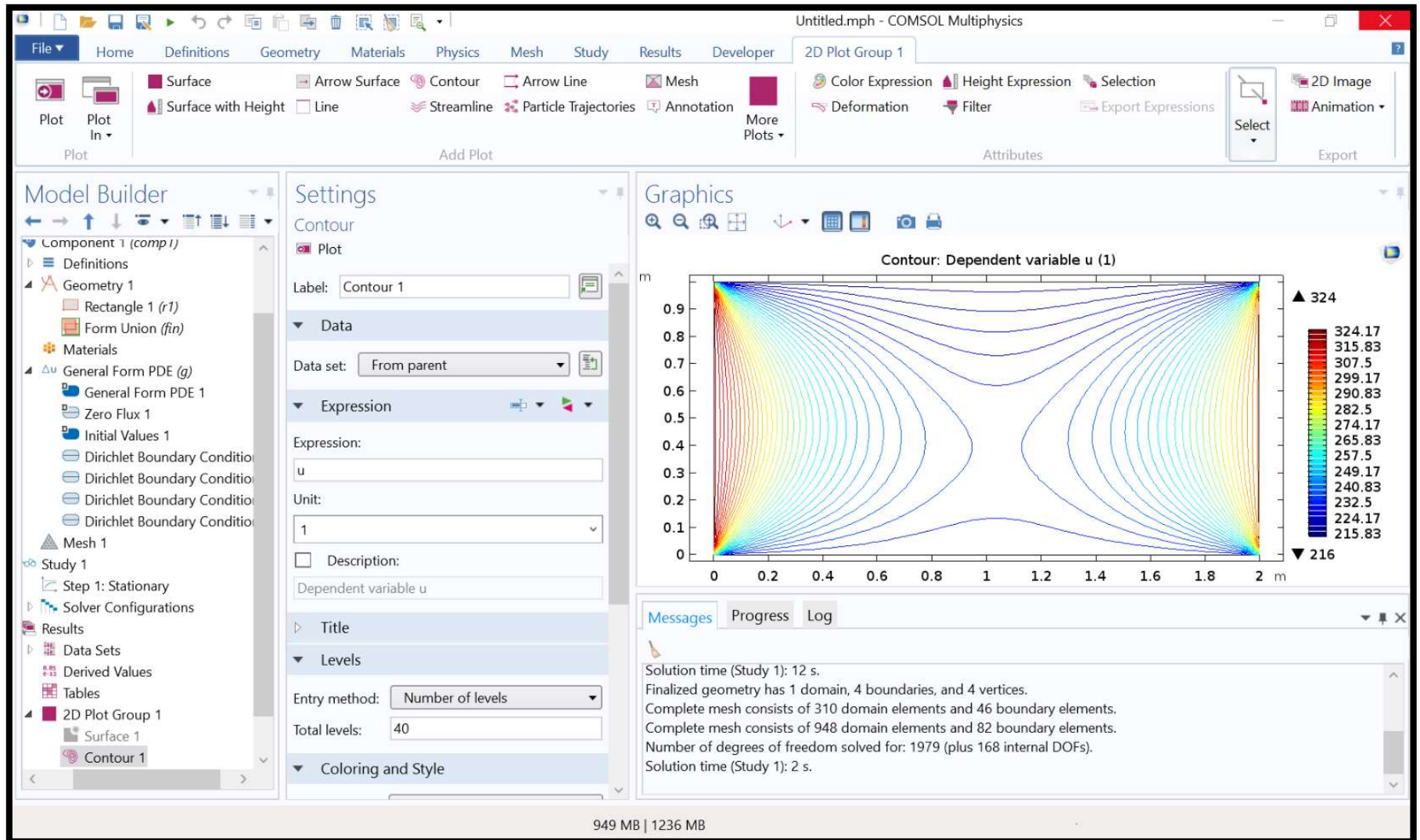
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 Complete mesh consists of 310 domain elements and 46 boundary elements.
 Complete mesh consists of 948 domain elements and 82 boundary elements.

723 MB | 1233 MB









Untitled.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer 2D Plot Group 1

Plot Plot In Plot Add Plot Attributes Export

Surface Arrow Surface Contour Arrow Line Mesh Color Expression Height Expression Selection Deformation Filter Export Expressions 2D Image Animation

Model Builder

- Component 1 (comp 1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Dirichlet Boundary Condition 1
 - Dirichlet Boundary Condition 2
 - Dirichlet Boundary Condition 3
 - Dirichlet Boundary Condition 4
 - Mesh 1
 - Study 1
 - Step 1: Stationary
 - Solver Configurations
 - Results
 - Data Sets
 - Derived Values
 - Tables
 - 2D Plot Group 1
 - Surface 1
 - Contour 1

Settings

Surface

Plot

Expression: u

Unit: 1

Description: Dependent variable u

Title

Range

Coloring and Style

Coloring: Color table

Color table: Thermal

Color legend

Reverse color table

Symmetrize color range

Wireframe

Quality

Inherit Style

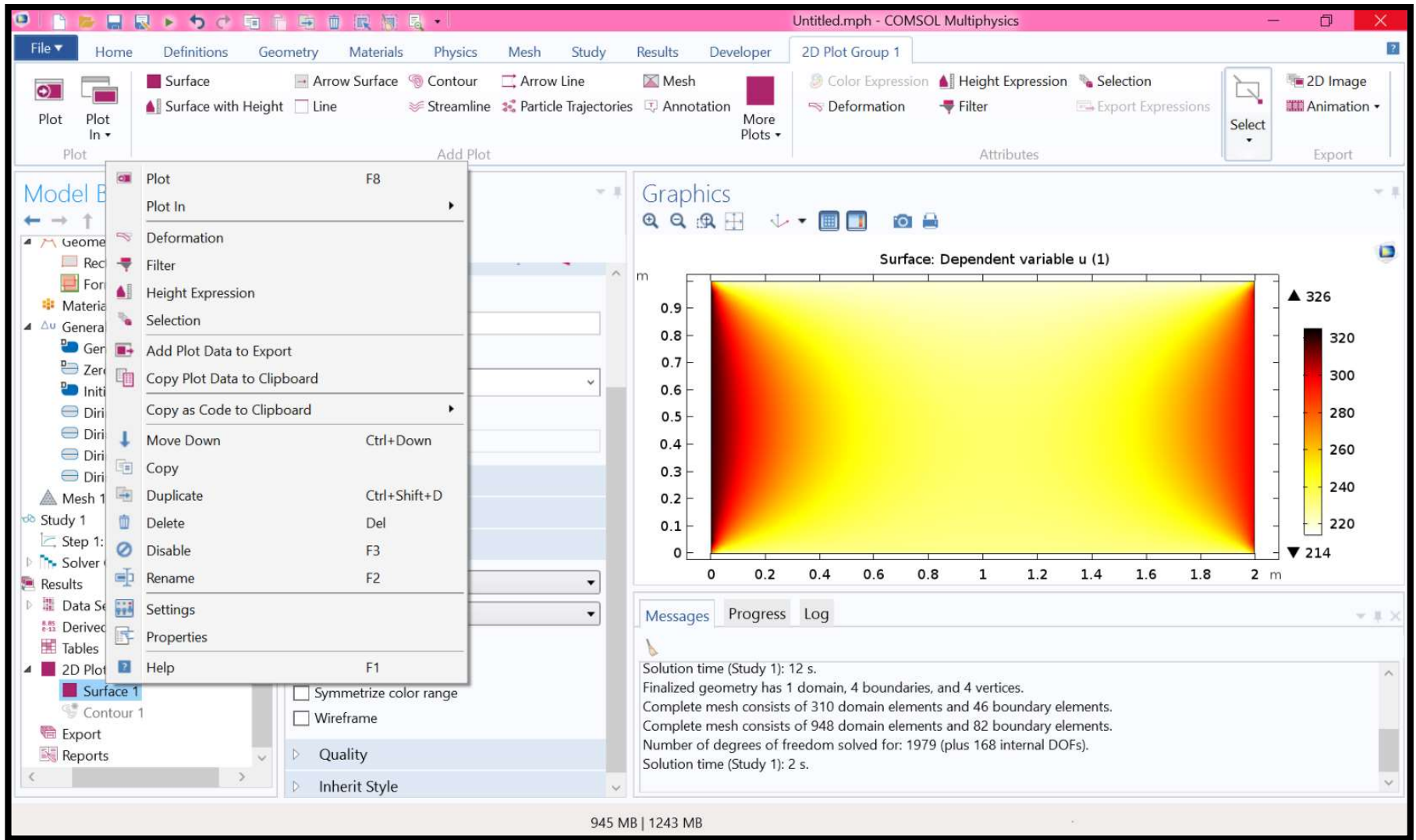
Graphics

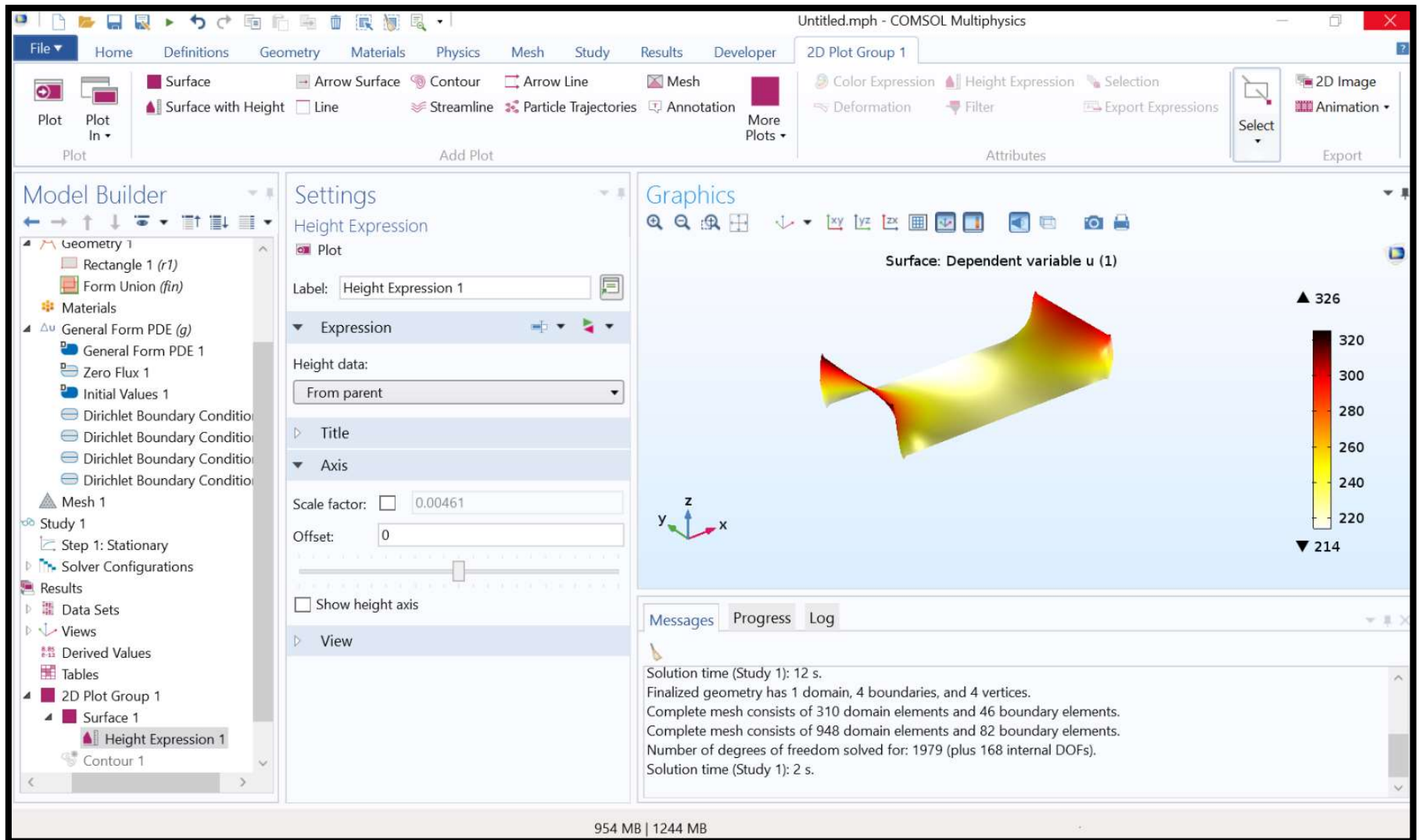
Surface: Dependent variable u (1)

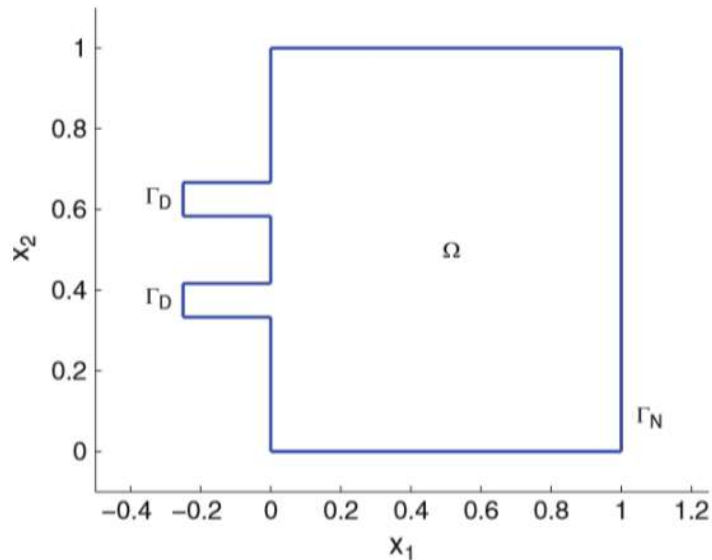
Messages Progress Log

Solution time (Study 1): 12 s.
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 Complete mesh consists of 310 domain elements and 46 boundary elements.
 Complete mesh consists of 948 domain elements and 82 boundary elements.
 Number of degrees of freedom solved for: 1979 (plus 168 internal DOFs).
 Solution time (Study 1): 2 s.

957 MB | 1246 MB







A MATLAB code for solving the Wave equation is given below. The problem under consideration is $\ddot{u} - \Delta u = 0$ in a domain Ω composed of a square with two smaller rectangular strips added on one side. This domain is shown in Fig. 5.3. The boundary conditions are $u = 0.1 \sin(8\pi t)$ on the line segments $\Gamma_D = \{x : x_1 = -0.25\}$, and $n \cdot \nabla u = 0$ on the rest of the boundary Γ_N . Thus, we have both Dirichlet and Neumann boundary conditions. The initial condition u_0 is zero.

Select Physics

Search

- Recently Used
 - General Form PDE (g)
 - Heat Transfer in Solids (ht)
 - Heat Equation (hreq)
 - Laminar Flow (spf)
 - Poisson's Equation (poeq)
- AC/DC
- Acoustics
- Chemical Species Transport
- Electrochemistry
- Fluid Flow
- Heat Transfer
- Optics
- Plasma

Add

Added physics interfaces:

General Form PDE (g)

Remove

← Space Dimension → Study

? Help X Cancel ✓ Done

Review Physics Interface

General Form PDE (g)

Dependent Variables

Field name:

Number of dependent variables:

Dependent variables:

u

+ ≡

Units

— Dependent variable quantity —

— Source term quantity —

Unit:

Select Study

- ▾ Preset Studies
 - Eigenvalue
 - Stationary
 - Time Dependent ←
- Custom Studies
- Empty Study

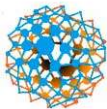
Added study:

Added physics interfaces:

△v General Form PDE (g)

← Physics

? Help × Cancel ✓ Done



CEMIAC

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Application Builder Component Model

Parameters Functions Variables

Geometry Materials

General Form PDE Build Mesh Compute Add Study Select Plot Group Windows

Add Physics Mesh 1 Study 1 Add Plot Group Reset Desktop

Model Builder

Settings

Geometry

Build All

Label: Geometry 1

Units

Scale values when changing units

Length unit: m

Angular unit: Degrees

Advanced

Default repair tolerance: Automatic

Automatic rebuild

Graphics

Messages Progress Log

Saved file: C:\Users\Betty\Desktop\calor2D.mph
Saved file: C:\Users\Betty\Desktop\calor2D.mph
Saved file: C:\Users\Betty\Desktop\calor2D.mph
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Saved file: C:\Users\Betty\Desktop\calor2D.mph
Saved file: C:\Users\Betty\Desktop\ondaTaller.mph

913 MB | 1225 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Tangent Fillet Virtual Operations Parts Programming Other

Model Builder

- ondaTaller.mph (root)
 - Global Definitions
 - Materials
 - Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - Mesh 1
 - Study 1
 - Results

Settings

Rectangle

Build Selected Build All Objects

Label: Rectangle 1

Object Type

Type: Solid

Size and Shape

Width: 1 m

Height: 1 m

Position

Base: Corner

x: 0 m

y: 0 m

Rotation Angle

Rotation: 0 deg

Layers

Selections of Resulting Entities

Contribute to: None New

Graphics

Messages Progress Log

COMSOL Multiphysics 5.3.0.260
Opened file: C:\Users\Betty\Desktop\ondaTaller.mph

740 MB | 887 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder Settings Graphics

ondaTaller.mph (root)

- Global Definitions
- Materials
- Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - Mesh 1
 - Study 1
 - Results

Rectangle

Build Selected Build All Objects

Label: Rectangle 2

Object Type

Type: Solid

Size and Shape

Width: 0.2 m

Height: 0.1 m

Position

Base: Corner

x: -0.2 m

y: 0.3 m

Rotation Angle

Rotation: 0 deg

Layers

Selections of Resulting Entities

Contribute to: None New

Graphics

Messages Progress Log

COMSOL Multiphysics 5.3.0.260
Opened file: C:\Users\Betty\Desktop\ondaTaller.mph

736 MB | 879 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder

- ondaTaller.mph (root)
 - Global Definitions
 - Materials
 - Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - Mesh 1
 - Study 1
 - Results

Settings

Rectangle

Build Selected Build All Objects

Label: Rectangle 3

Object Type

Type: Solid

Size and Shape

Width: 0.2 m

Height: 0.1 m

Position

Base: Corner

x: -0.2 m

y: 0.6 m

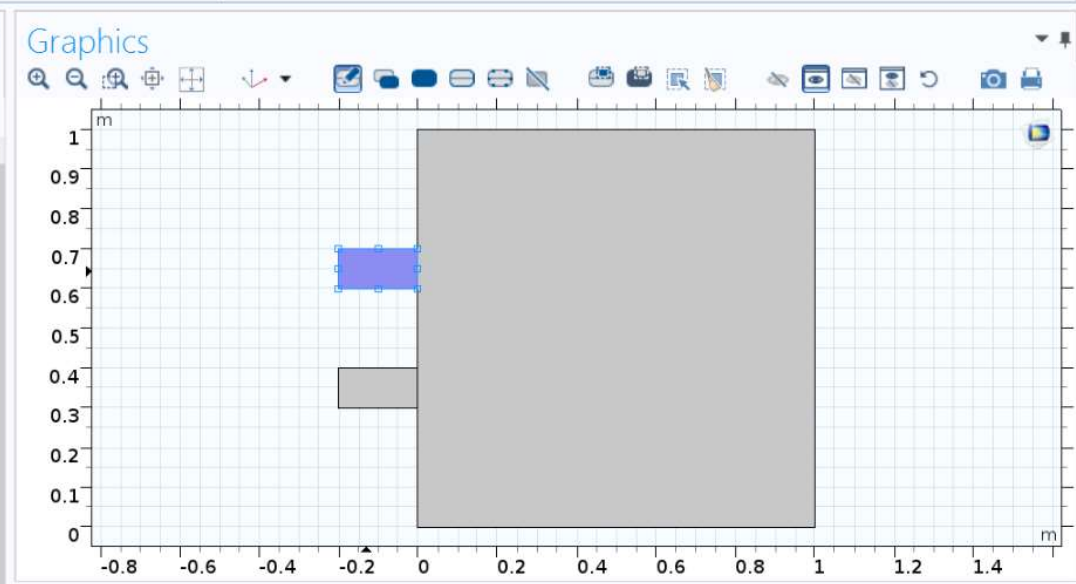
Rotation Angle

Rotation: 0 deg

Layers

Selections of Resulting Entities

Contribute to: None New



Messages Progress Log

COMSOL Multiphysics 5.3.0.260
Opened file: C:\Users\Betty\Desktop\ondaTaller.mph

745 MB | 882 MB



ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives **Booleans and Partitions** Transforms Conversions Chamfer Tangent Fillet Virtual Operations Parts Programming Other

Draw Operations Other

Model Builder

- ondaTaller.mph (root)
 - Global Definitions
 - Materials
 - Component 1 (comp1)
 - Definitions
 - Geometry 1**
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - Mesh 1
 - Study 1
 - Results

Settings

Geometry

Build All

Label: Geometry 1

Units

Scale values when changing units

Length unit: m

Angular unit: Degrees

Advanced

Default repair tolerance: Automatic

Automatic rebuild

Union

Intersection

Difference

Compose

Partition Objects

Partition Domains

Partition Edges

Graphics

Messages Progress Log

COMSOL Multiphysics 5.3.0.260
Opened file: C:\Users\Betty\Desktop\ondaTaller.mph

730 MB | 875 MB



ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder Settings Graphics

ondaTaller.mph (root)

- Global Definitions
- Materials
- Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Union 1 (uni1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - Mesh 1
 - Study 1
 - Results

Union

Build Selected Build All Objects

Label: Union 1

Input objects:

Active: r1, r2, r3

Keep input objects:

Keep interior boundaries:

Repair tolerance: Automatic

Selections of Resulting Entities

Contribute to: None New

Resulting objects selection:

Show in physics: Domain selection

Graphics

Messages Progress Log

COMSOL Multiphysics 5.3.0.260
Opened file: C:\Users\Betty\Desktop\ondaTaller.mph

734 MB | 883 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder Settings Graphics

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- Global Definitions
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 - Rectangle 3 (r3)
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 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - Mesh 1
 - Study 1
 - Results

Union

Build Selected Build All Objects

Label: Union 1

Union

Input objects:

OFF r1

OFF r2

Active r3

Keep input objects

Keep interior boundaries

Repair tolerance: Automatic

Selections of Resulting Entities

Contribute to: None New

Resulting objects selection

Show in physics: Domain selection

Graphics

Messages Progress Log

COMSOL Multiphysics 5.3.0.260

Opened file: C:\Users\Betty\Desktop\ondaTaller.mph

727 MB | 896 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder

- ondaTaller.mph (root)
 - Global Definitions
 - Materials
 - Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Union 1 (uni1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Mesh 1
 - Study 1
 - Results

Settings

General Form PDE

Override and Contribution

Equation

Show equation assuming:

Study 1, Time Dependent

$$e_a \frac{\partial^2 u}{\partial t^2} + d_a \frac{\partial u}{\partial t} + \nabla \cdot \Gamma = f$$

$$\nabla = \left[\frac{\partial}{\partial x}, \frac{\partial}{\partial y} \right]$$

Conservative Flux

Γ_x	-ux	x	1/m
Γ_y	-uy	y	

Source Term

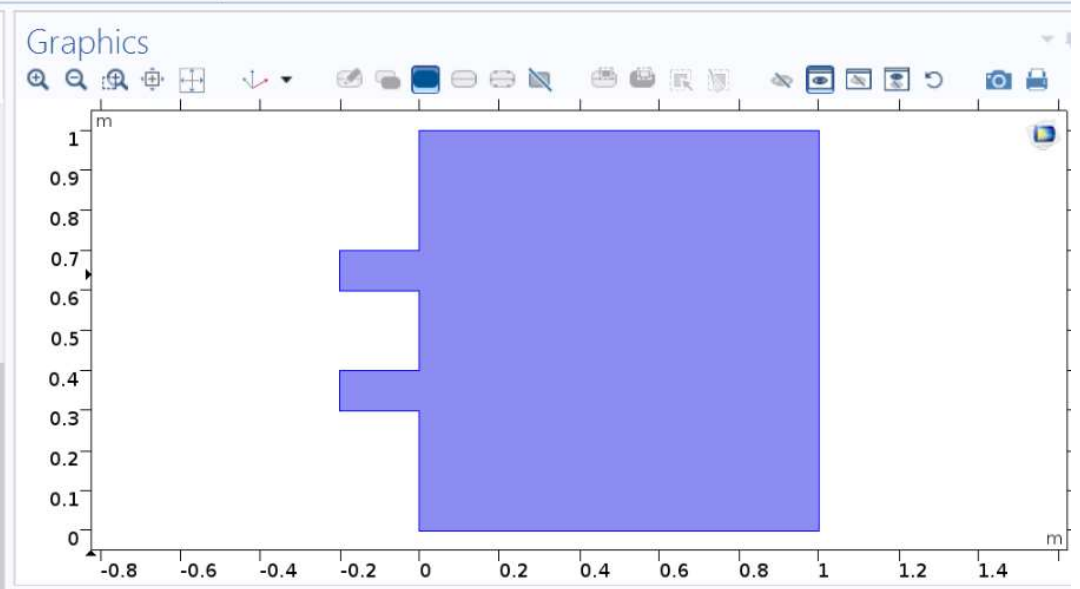
f 1 1/m²

Damping or Mass Coefficient

d_a 1 s/m²

Mass Coefficient

e_a 0 s²/m²



Messages Progress Log

COMSOL Multiphysics 5.3.0.260
 Opened file: C:\Users\Betty\Desktop\ondaTaller.mph
 Finalized geometry has 1 domain, 12 boundaries, and 12 vertices.

760 MB | 904 MB



The problem under consideration is $\ddot{u} - \Delta u = 0$ in a domain Ω composed of a square with two smaller rectangular strips added on one side. This domain is shown in Fig. 5.3. The boundary conditions are $u = 0.1 \sin(8\pi t)$ on the line segments $\Gamma_D = \{x : x_1 = -0.25\}$, and $n \cdot \nabla u = 0$ on the rest of the boundary Γ_N . Thus, we have both Dirichlet and Neumann boundary conditions. The initial condition u_0 is zero.

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder

- ondaTaller.mph (root)
 - Global Definitions
 - Materials
 - Component 1 (comp1)
 - Definitions
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 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Union 1 (uni1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Dirichlet Boundary Con
 - Mesh 1
 - Study 1
 - Results

Settings

General Form PDE

Override and Contribution

Equation

Show equation assuming:
Study 1, Time Dependent

$$e_a \frac{\partial^2 u}{\partial t^2} + d_a \frac{\partial u}{\partial t} + \nabla \cdot \Gamma = f$$

$$\nabla = \left[\frac{\partial}{\partial x}, \frac{\partial}{\partial y} \right]$$

Conservative Flux

Γ_x	-ux	x	1/m
Γ_y	-uy	y	

Source Term

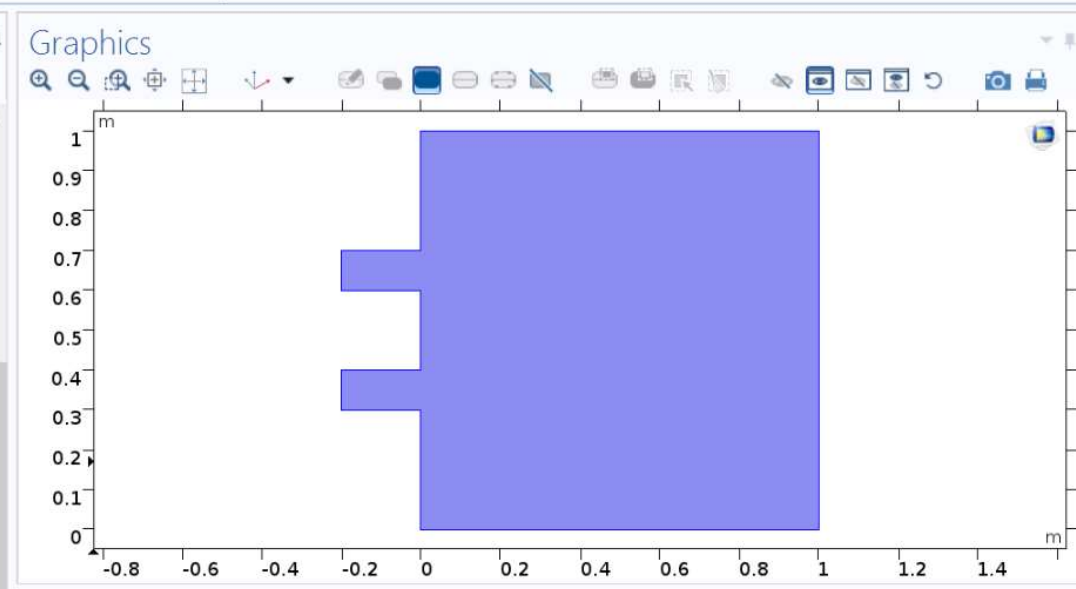
f 0 1/m²

Damping or Mass Coefficient

d_a 0 s/m²

Mass Coefficient

e_a 1 s²/m²



Messages Progress Log

COMSOL Multiphysics 5.3.0.260
 Opened file: C:\Users\Betty\Desktop\ondaTaller.mph
 Finalized geometry has 1 domain, 12 boundaries, and 12 vertices.

516 MB | 916 MB



ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder

- ondaTaller.mph (root)
 - Global Definitions
 - Materials
 - Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Union 1 (uni1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Dirichlet Boundary Condition 1
 - Mesh 1
 - Study 1
 - Results

Settings

Dirichlet Boundary Condition

Label: Dirichlet Boundary Condition 1

Boundary Selection

Selection: Manual

<input checked="" type="checkbox"/>	1
<input checked="" type="checkbox"/>	4

Active

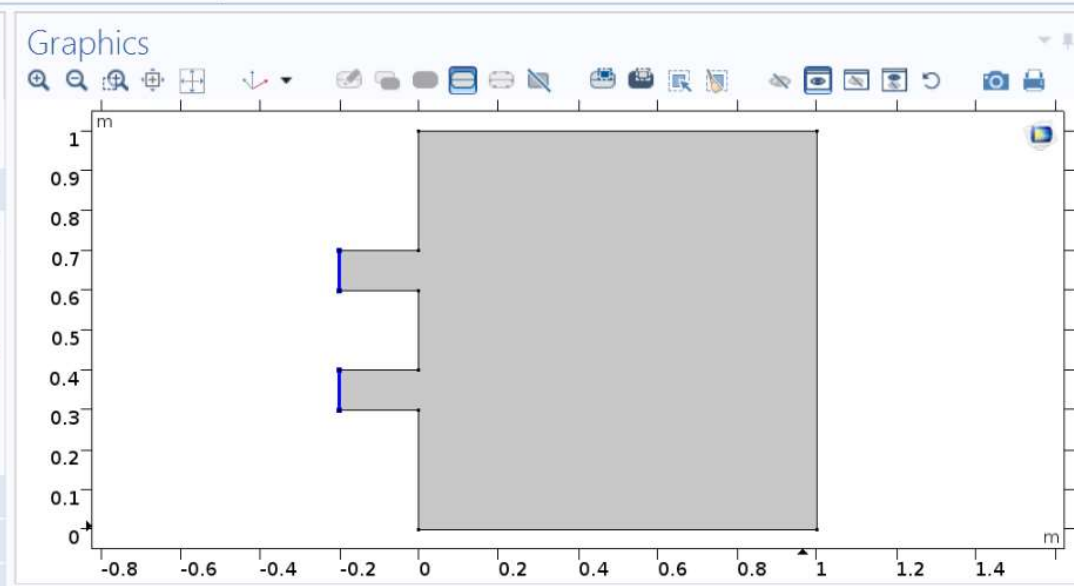
Override and Contribution

Equation

Dirichlet Boundary Condition

Prescribed value of u

r 1



Messages Progress Log

COMSOL Multiphysics 5.3.0.260
 Opened file: C:\Users\Betty\Desktop\ondaTaller.mph
 Finalized geometry has 1 domain, 12 boundaries, and 12 vertices.

536 MB | 925 MB



ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder Settings Graphics

ondaTaller.mph (root)
 Global Definitions
 Materials
 Component 1 (comp1)
 Definitions
 Geometry 1
 Rectangle 1 (r1)
 Rectangle 2 (r2)
 Rectangle 3 (r3)
 Union 1 (uni1)
 Form Union (fn)
 Materials
 General Form PDE (g)
 General Form PDE 1
 Zero Flux 1
 Initial Values 1
 Dirichlet Boundary Condition 1
 Mesh 1
 Study 1
 Results

Settings
 Zero Flux
 Label: Zero Flux 1
 Boundary Selection
 Selection: All boundaries
 Active: 1 (overridden), 2, 3, 4 (overridden), 5, 6
 Override and Contribution
 Equation

Graphics
 1 m
 0.9
 0.8
 0.7
 0.6
 0.5
 0.4
 0.3
 0.2
 0.1
 0
 -0.8 -0.6 -0.4 -0.2 0 0.2 0.4 0.6 0.8 1 1.2 1.4 m

Messages Progress Log
 COMSOL Multiphysics 5.3.0.260
 Opened file: C:\Users\Betty\Desktop\ondaTaller.mph
 Finalized geometry has 1 domain, 12 boundaries, and 12 vertices.

535 MB | 919 MB



ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder Settings Graphics

Initial Values

Label: Initial Values 1

Domain Selection

Selection: All domains

Active

Override and Contribution

Initial Values

Initial value for u: 0 1

Initial time derivative of u: $\frac{du}{dt}$ 0 1/s

Messages Progress Log

COMSOL Multiphysics 5.3.0.260
 Opened file: C:\Users\Betty\Desktop\ondaTaller.mph
 Finalized geometry has 1 domain, 12 boundaries, and 12 vertices.

529 MB | 921 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Build Import/Export Draw Settings Line Rectangle Circle Primitives Booleans and Partitions Transforms Conversions Chamfer Fillet Tangent Virtual Operations Parts Programming Other

Model Builder Settings Graphics

Mesh

Build All

Label: Mesh 1

Mesh Settings

Sequence type: Physics-controlled mesh

Element size: Finer

Messages Progress Log

COMSOL Multiphysics 5.3.0.260
 Opened file: C:\Users\Betty\Desktop\ondaTaller.mph
 Finalized geometry has 1 domain, 12 boundaries, and 12 vertices.
 Complete mesh consists of 480 domain elements and 66 boundary elements.
 Complete mesh consists of 1444 domain elements and 114 boundary elements.

516 MB | 876 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Application Builder Component Parameters Functions Variables Geometry Materials

General Form PDE Build Mesh Compute Add Study 2D Plot Group 1 Windows

Add Physics Mesh 1 Study 1 Add Plot Group Reset Desktop

Application Model Definitions Physics Mesh Study Results Layout

Model Builder

- Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Union 1 (uni1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Dirichlet Boundary C
 - Mesh 1
 - Study 1
 - Step 1: Time Dependent
 - Solver Configurations
 - Results
 - Data Sets
 - Derived Values
 - Tables
 - 2D Plot Group 1
 - Surface 1
 - Export

Settings

Time Dependent

Compute Update Solution

Label: Time Dependent

Study Settings

Time unit: s

Times: range(0,0.005,2) s

Tolerance: Physics controlled

Results While Solving

Physics and Variables Selection

Modify physics tree and variables for study step

Physics interface	Sc	Discretization
General Form PDE (g)	<input checked="" type="checkbox"/>	Physics settings

Values of Dependent Variables

Mesh Selection

Study Extensions

Graphics Convergence Plot 1

Messages Progress Log

Complete mesh consists of 480 domain elements and 66 boundary elements.
 Complete mesh consists of 1444 domain elements and 114 boundary elements.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 23 s.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 19 s.

797 MB | 981 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer 2D Plot Group 1

Plot Plot In Surface Surface with Height Arrow Surface Contour Arrow Line Mesh Color Expression Height Expression Selection Deformation Filter Export Expressions 2D Image Animation

Model Builder

- Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Union 1 (uni1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Dirichlet Boundary C
 - Mesh 1
 - Study 1
 - Step 1: Time Dependent
 - Solver Configurations
 - Results
 - Data Sets
 - Derived Values
 - Tables
 - 2D Plot Group 1
 - Surface 1

Settings

2D Plot Group

Plot

Label: 2D Plot Group 1

Data

Data set: Study 1/Solution 1 (sol1)

Time (s): 2

Title

Plot Settings

View: Automatic

x-axis label:

y-axis label:

Show hidden entities

Propagate hiding to lower dimensions

Plot data set edges

Color: Black

Frame: Material (X, Y, Z)

Color Legend

Graphics

Convergence Plot 1

Time=2 s Surface: Dependent variable u (1)

Messages Progress Log

Complete mesh consists of 480 domain elements and 66 boundary elements.
 Complete mesh consists of 1444 domain elements and 114 boundary elements.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 23 s.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 19 s.

801 MB | 987 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer 2D Plot Group 1

Plot Plot In Surface Arrow Surface Contour Arrow Line Mesh Color Expression Height Expression Selection Deformation Filter Export Expressions 2D Image Animation

Plot Add Plot Attributes Export

Model Builder

- Component 1 (comp1)
 - Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Union 1 (uni1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Dirichlet Boundary C
 - Mesh 1
 - Study 1
 - Step 1: Time Dependent
 - Solver Configurations
 - Results
 - Data Sets
 - Derived Values
 - Tables
 - 2D Plot Group 1
 - Surface 1

Settings

2D Plot Group

Plot

Label: 2D Plot Group 1

Data

Data set: Study 1/Solution 1 (sol1)

Time (s): 1.205

Title

Plot Settings

View: Automatic

x-axis label:

y-axis label:

Show hidden entities

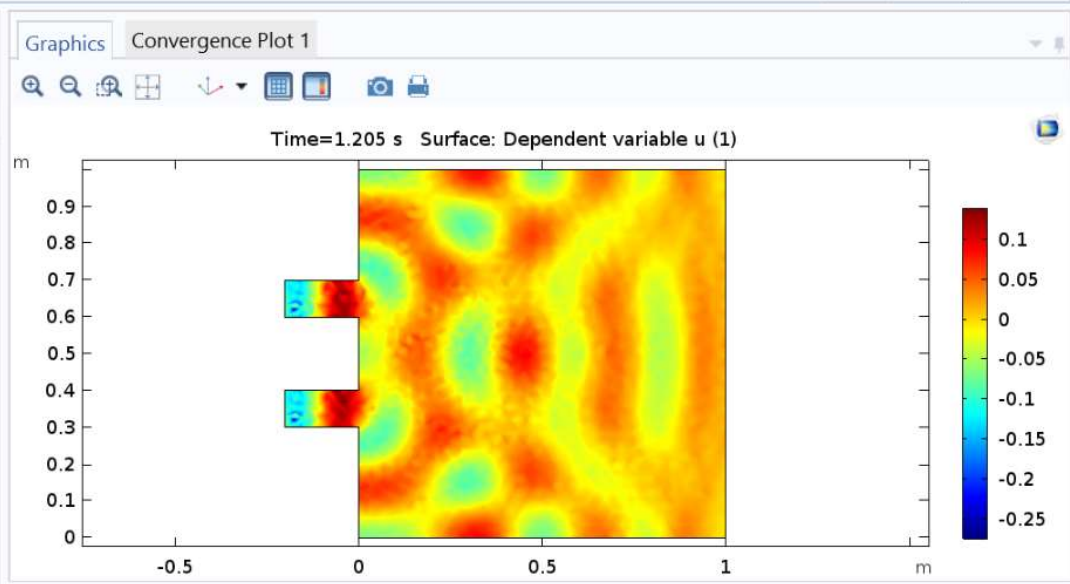
Propagate hiding to lower dimensions

Plot data set edges

Color: Black

Frame: Material (X, Y, Z)

Color Legend



Messages Progress Log

Complete mesh consists of 480 domain elements and 66 boundary elements.
 Complete mesh consists of 1444 domain elements and 114 boundary elements.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 23 s.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 19 s.

801 MB | 979 MB



ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer 2D Plot Group 1

Plot Plot In Surface Surface with Height Line Arrow Surface Contour Arrow Line Mesh Color Expression Height Expression Selection Deformation Filter Export Expressions 2D Image Animation

Model Builder Settings Surface

Component 1 (c) Definitions Geometry 1 Rectangle Rectangle Rectangle Union 1 Form Un Materials General Form General F Zero Flux Initial Val Dirichlet Mesh 1 Study 1 Step 1: Time Solver Conf Results Data Sets Derived Valu Tables 2D Plot Group Surface 1

Plot Plot In Deformation Filter Height Expression Selection Add Plot Data to Export Copy Plot Data to Clipboard Copy as Code to Clipboard Copy Duplicate Delete Disable Rename Settings Properties Help

Coloring: Color table Color table Color table

Color table: Rainbow

Color legend

Graphics Convergence Plot 1

Time=2 s Surface: Dependent variable u (1)

Messages Progress Log

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 Solution time (Study 1): 19 s.

796 MB | 981 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer 2D Plot Group 1

Plot Plot In Surface Arrow Surface Contour Arrow Line Mesh Color Expression Height Expression Selection Deformation Filter Export Expressions 2D Image Animation

Model Builder

- Definitions
 - Geometry 1
 - Rectangle 1 (r1)
 - Rectangle 2 (r2)
 - Rectangle 3 (r3)
 - Union 1 (uni1)
 - Form Union (fin)
 - Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Dirichlet Boundary C
 - Mesh 1
 - Study 1
 - Step 1: Time Dependent
 - Solver Configurations
 - Results
 - Data Sets
 - Views
 - Derived Values
 - Tables
 - 2D Plot Group 1
 - Surface 1
 - Height Expression

Settings

2D Plot Group

Plot

Plot Settings

View: Automatic

x-axis label:

y-axis label:

Show hidden entities

Propagate hiding to lower dimensions

Plot data set edges

Color: Black

Frame: Material (X, Y, Z)

Color Legend

Show legends

Show maximum and minimum values

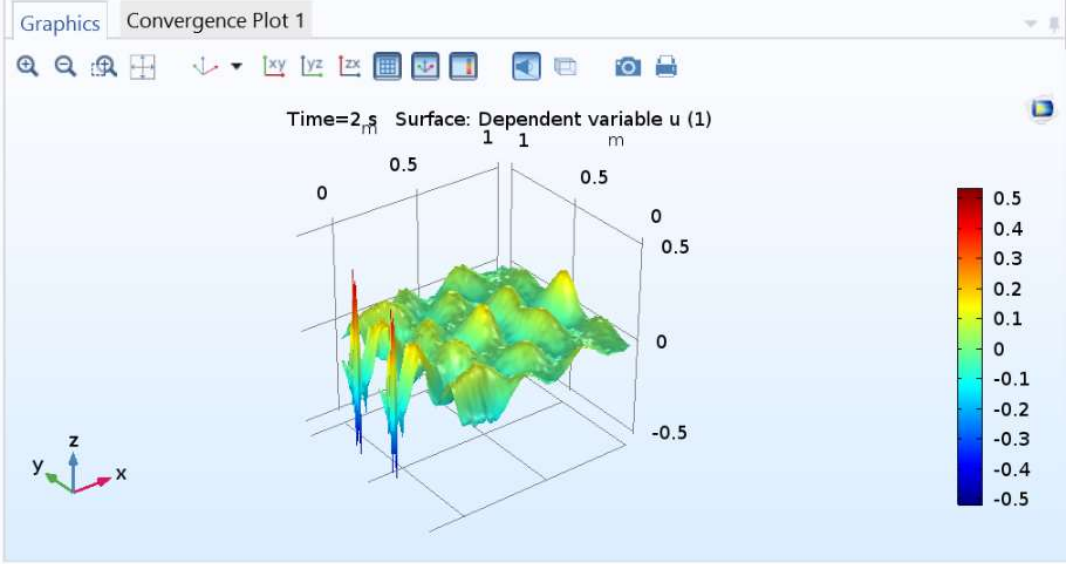
Show units

Position: Right

Text color: Black

Number Format

Window Settings



Messages Progress Log

Complete mesh consists of 480 domain elements and 66 boundary elements.
 Complete mesh consists of 1444 domain elements and 114 boundary elements.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 23 s.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 19 s.

812 MB | 985 MB



ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer 2D Plot Group 1

Plot Plot In Surface Arrow Surface Contour Arrow Line Mesh Color Expression Height Expression Selection Deformation Filter Export Expressions 2D Image Animation

Model Builder Settings Graphics Convergence Plot 1

2D Plot Group

Plot Settings

View: Automatic

x-axis label: y-axis label:

Show hidden entities Propagate hiding to lower dimensions Plot data set edges

Color: Black Frame: Material (X, Y, Z)

Color Legend

Show legends Show maximum and minimum values Show units

Position: Right Text color: Black

Number Format Window Settings

Time=2 s Surface: Dependent variable u (1)

Messages Progress Log

Complete mesh consists of 480 domain elements and 66 boundary elements.
 Complete mesh consists of 1444 domain elements and 114 boundary elements.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 23 s.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 19 s.

806 MB | 988 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Plot 2D Plot Group 1 3D Plot Group 2D Plot Group 1D Plot Group Polar Plot Group Smith Plot Group Parameters Definitions

Cut Plane Cut Line 3D More Data Sets Selection Remesh Deformed Configuration Derived Values Table Data Animation Player File Report

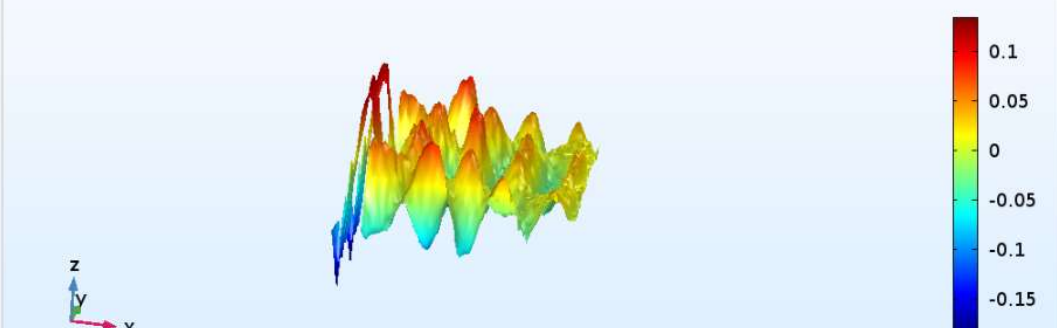
Model Builder Settings Graphics Convergence Plot 1

Results

Result Settings

Automatic update of plots

Time=1.2 s Surface: Dependent variable u (1)



Messages Progress Log

Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
Solution time (Study 1): 23 s.
Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
Solution time (Study 1): 19 s.
Saved file: C:\Users\Betty\Desktop\ondaTaller.mph
Mesh error (map1): Failed to create mapped mesh for domain.
Complete mesh consists of 1444 domain elements and 114 boundary elements.

817 MB | 983 MB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Plot 2D Plot Group 1 3D Plot Group 2D Plot Group 1D Plot Group Polar Plot Group Smith Plot Group Parameters Definitions

Cut Plane Cut Line 3D More Data Sets Selection Remesh Deformed Configuration Derived Values Table Data Animation Image Report Export

8.85 e-12

Model Builder

- Rectangle 2 (r2)
- Rectangle 3 (r3)
- Union 1 (uni1)
- Form Union (fin)
- Materials
- General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Dirichlet Boundary Conc
- Mesh 1
- Study 1
 - Step 1: Time Dependent
 - Solver Configurations
 - Results
 - Data Sets
 - Views
 - Derived Values
 - Tables
 - 2D Plot Group 1
 - Surface 1
 - Height Expression 1
 - Export
 - Animation 1
 - Animation 2

Settings

Animation

Refresh Export

Label: Animation 2

Scene

Subject: 2D Plot Group 1

Target

Target: File

Output

Output type: Movie

Format: GIF

Filename: Browse...

Always ask for filename

Open in browser

Frames per second: 10

Animation Editing

Sequence type: Stored solutions

Loop over: Time

Graphics

Convergence Plot 1

Time=1.2 s Surface: Dependent variable u (1)

z y x

0.1
0.05
0
-0.05
-0.1
-0.15

Messages Progress Log

Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 23 s.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 19 s.
 Saved file: C:\Users\Betty\Desktop\ondaTaller.mph
 Mesh error (map1): Failed to create mapped mesh for domain.
 Complete mesh consists of 1444 domain elements and 114 boundary elements.

1.02 GB | 1.19 GB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Plot 2D Plot Group 1 3D Plot Group 2D Plot Group 1D Plot Group Polar Plot Group Smith Plot Group Parameters Pi Definitions

Cut Plane Cut Line 3D More Data Sets Selection Remesh Deformed Configuration Derived Values Table Data Animation Image Report Export

8.85 e-12

Model Builder

- Rectangle 2 (r2)
- Rectangle 3 (r3)
- Union 1 (uni1)
- Form Union (fin)
- Materials
 - General Form PDE (g)
 - General Form PDE 1
 - Zero Flux 1
 - Initial Values 1
 - Dirichlet Boundary Conc
 - Mesh 1
- Study 1
 - Step 1: Time Dependent
 - Solver Configurations
 - Results
 - Data Sets
 - Views
 - Derived Values
 - Tables
 - 2D Plot Group 1
 - Surface 1
 - Height Expression 1
 - Export
 - Animation 1
 - Animation 2

Settings

Animation

Refresh Export

Time selection: All

Frames

Frame selection: Number of frames

Number of frames: 200

Size: Manual

Lock aspect ratio

Width: 640 px

Height: 480 px

Record in reverse order

Layout

Include

Title

Color legend

Grid

Axis orientation

Logotype

Font size: 9 pt

Graphics Convergence Plot 1

Time=1.2 s Surface: Dependent variable u (1)

Messages Progress Log

Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 23 s.
 Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 19 s.
 Saved file: C:\Users\Betty\Desktop\ondaTaller.mph
 Mesh error (map1): Failed to create mapped mesh for domain.
 Complete mesh consists of 1444 domain elements and 114 boundary elements.

1.06 GB | 1.22 GB

ondaTaller.mph - COMSOL Multiphysics

File Home Definitions Geometry Materials Physics Mesh Study Results Developer

Plot 2D Plot Group 1 3D Plot Group 2D Plot Group 1D Plot Group Polar Plot Group Smith Plot Group Parameters Pi More Data Sets Selection Remesh Deformed Configuration Derived Values Table Data Animation Image Report

Model Builder Settings Graphics Convergence Plot 1

Rectangle 2 (r2) Rectangle 3 (r3) Union 1 (uni1) Form Union (fin) Materials General Form PDE (g) General Form PDE 1 Zero Flux 1 Initial Values 1 Dirichlet Boundary Conc Mesh 1 Study 1 Step 1: Time Dependent Solver Configurations Results Data Sets Views Derived Values Tables 2D Plot Group 1 Surface 1 Height Expression 1 Export Animation 1 Animation 2

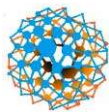
Animation Refresh Export Label: Animation 2 Scene Subject: 2D Plot Group 1 Target Target: File Output Output type: Movie Format: GIF Filename: C:\Users\Betty Browse... Always ask for filename Open in browser Frames per second: 10 Animation Editing Sequence type: Stored solutions Loop over: Time

Time=1.2 s Surface: Dependent variable u (1)

Messages Progress Log

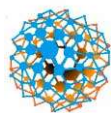
Number of degrees of freedom solved for: 3003 (plus 240 internal DOFs).
 Solution time (Study 1): 23 s.
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1.06 GB | 1.22 GB



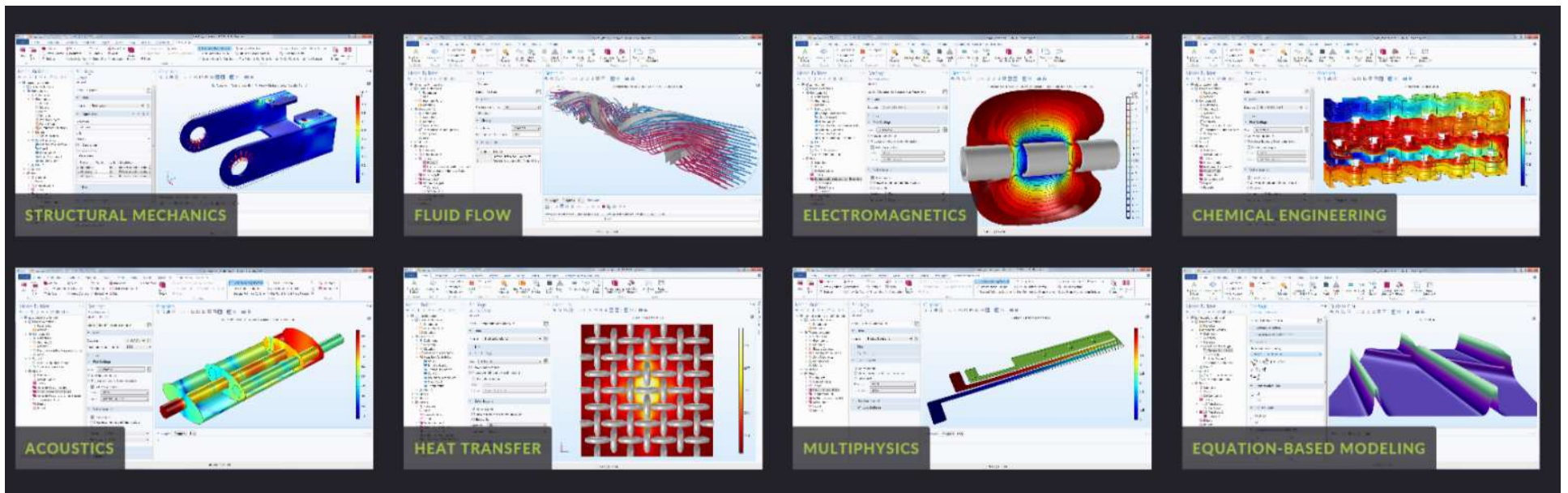
CEMIAC

<https://www.comsol.com/models>



CEMIAC

COMSOL Multiphysics



Tutoriales en youtube.

- <https://www.youtube.com/watch?v=qNc03bW18JE>
- <https://www.comsol.com/comsol-multiphysics>